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# Cognitive demands on geometrical tasks in Indonesian elementary school mathematics textbook

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#### Abstract

Examples and exercises in mathematics textbooks have an essential role in directing teaching and learning to achieve the objectives of the mathematics curriculum. This study examines mathematical tasks, i.e., examples and exercises, for a grade 4 elementary school mathematics textbook published by the Indonesian Government in 2018. We focus on geometry tasks and categorize them based on the dimensions of cognitive processes and knowledge of the revised Bloom's taxonomy. Textbook research is used to achieve the objectives of this study. The validity of the data was carried out by employing peer debriefing. The findings of this study indicate that only about 30% of the geometry tasks in this mathematics textbook require high-level mathematical thinking skills. This study also shows that procedural knowledge is more dominant and becomes an orientation in presenting geometry tasks. This finding becomes less relevant to the orientation of researchers and policymakers who want the direction of mathematics education to be forming students as problem solvers.

**Keywords:** Bloom taxonomy; elementary school; geometrical task; mathematics textbook; textbook research

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#### Introduction

Mathematics textbooks are descriptions of teaching materials in mathematics subjects that students and teachers use as a guide in carrying out the mathematics learning process, arranged systematically, and selected based on the objectives and achievements of learning mathematics (Muslich, 2010; Ramadhani, 2020). Mathematics textbooks must also be compiled and adapted to the applicable curriculum (Fan, 2013) and have great potential in determining the teaching and learning process in the classroom (Aldahmash et al., 2016; Fan et al., 2013; Wijaya et al., 2015). Once the role of textbooks is so essential, it is natural that textbooks have experienced increased attention in mathematics education research in the past two decades (Fan, 2013; Trouche & Fan, 2018). More than that, textbooks are essential to explore, in addition to finding the best formula for how the learning objectives or curriculum are achieved, but also used to streamline the role of the textbooks themselves because most teachers still rely on mathematics textbooks to carry out mathematics learning in the classroom either in planning, process, and evaluation (Kilpatrick et al., 2001; Purnomo et al., 2016; Sugiatno & Husna, 2020).

Examples and exercises are a significant aspect of mathematics textbooks and the focus of emphasis in textbook research (Bingolbali, 2020; Gracin, 2018; Purnomo, Mastura, et al., 2019). This portion is typically, but not always, used to practice skills, boost engagement, and as a tool for evaluation. As a result, the cognitive demands in this area are critical in order to fit with these intended aims and expectations.

Some researchers refer to the level of cognitive demands based on Stein and colleagues' work (Stein et al., 2000), specifically memorization, procedures without connections, procedures with connections, and doing mathematics (Charalambous et al., 2010; Hong & Choi, 2014; Yang & Sianturi, 2017, 2020). The first two levels belong to the low level, while the next two correspond to the high level. The OECD framework (OECD, 2010), which encompasses reproduction, connection, and reflection, is used in other works (Gracin, 2018; Wijaya et al., 2015, 2018). The reproduction level is related to the first two levels of Stein and colleagues' level, which are memorization and procedures without connections, whereas the others are types. Some researchers utilize Revised Bloom's taxonomy to classify the cognitive demands of their research area, which is related to another idea (Johar et al., 2017; Kul et al., 2018). Revised Bloom's taxonomy has two dimensions: the cognitive process dimension and the knowledge dimension. The dimensions of cognitive processes are activities performed to attain goals such as remembering (C1), understanding (C2), applying (C3), analyzing (C4), assessing (C5), and creating (C6). The knowledge dimension refers to knowledge acquired, such as facts, concepts, principles, procedures, and metacognition (Anderson & Krathwohl, 2001). We favor Revised Bloom's framework as a reference for cognitive leveling since it is more complete and familiar in the cognitive research area and focus on one of the materials: geometry tasks in fourth grade.

Some empirical evidence shows that geometry is one of the topics in mathematics that is challenging (Annizar et al., 2020; Pramudiani et al., 2017) and rarely becomes the focus of research, especially in textbook research (Chang & Silalahi, 2017; Purnomo, Mastura, et al., 2019). In contrast, geometry is one of the basic competencies in the curriculum for every basic

education level. However, several studies in Indonesia have not focused much on textbook research, particularly regarding the level of cognition and knowledge of geometry supplied by primary school mathematics textbooks in Indonesia. This study is significant because Indonesian education policy focuses on how to construct HOTs rather than LOTs to meet the changes and challenges of global advancement. As a result, this study aims to examine geometry textbooks for 4th-grade elementary school students based on cognitive processes and knowledge in examples and exercises.

# Methods

This research is a qualitative type of research that uses content analysis techniques. Leedy and Ormrod (2015) state that content analysis is a systematic and in-depth examination of the content of a particular material to identify patterns, themes, and biases. Because the focus is on textbooks, we are more comfortable using the term textbook research for this study (Fan et al., 2013; Fan, 2013; Purnomo, Mastura, et al., 2019; Rahmawati et al., 2020). The analysis chosen is to analyze one textbook with one specific topic, namely plane geometry. The object of the textbook that is analyzed is a mathematical task that includes worked examples and exercises.

We analyzed one mathematics textbook for grade 4 elementary school with curriculum 2013 revision (latest curriculum). This textbook is an electronic school textbook published by the Government, namely the Book Center of the Ministry of Education and Culture of the Republic of Indonesia. Electronic school textbooks are one of the Indonesian Government's programs launched in 2008 to provide quality, inexpensive, affordable schoolbooks that meet national standards. All copyrights for electronic school textbooks are purchased by the Government and can be downloaded for free in Portable Document Format (PDF) on the <a href="https://bse.learning.kemdikbud.go.id/">https://bse.learning.kemdikbud.go.id/</a> site. The textbook was chosen because it has been provided by the Government as a guide in learning mathematics and has become the main reference in learning mathematics in schools in Indonesia.

Textbook analysis was carried out by referring to the framework of the revised edition of Bloom's taxonomy (Anderson & Krathwohl, 2001). In the Bloom's revised taxonomy, there are two dimensions of the framework, namely the dimensions of cognitive processes and knowledge. The classification and coding for each level in the two dimensions and the respective examples are displayed in Table 1 (Anderson & Krathwohl, 2001; Kul et al., 2018).

Level	Description	Example <sup>*</sup>	Code
Dimensions of Cognitive Process			
Level 1	Retrieve relevant knowledge	What is perimeter?	C1
(Remembering)	from memory (remembering,	What is area?	
	recognizing)		
Level 2	Building meaning from the	What are the perimeters and areas	C2
(Understanding)	learning process, including	of these two shapes?	
	oral, written, drawing		
	communication (interpreting,		
	exemplifying, summarizing)		

Table 1. Coding for frameworks in the revised Bloom's Taxonomy

Level	Description	Example*	Code
Dimensions of Co	ognitive Process		
Level 3 (Applying)	In the situation at hand, do or employ the procedure (using, carrying out, implementing).	How do the perimeters and areas of these two shapes compare?	C3
Level 4 (Analyzing)	Break down a substance into its component elements and figure out how they connect to one another and to a larger structure or purpose (organizing, sorting, grouping, rearranging).	If you increase the width of a rectangle by 2 units, what happens to the area and perimeter?	C4
Level 5 (Evaluating)	Make judgments/assessments based on criteria and standards (checking, judging, critiquing)	Which floor plan provides a larger seating capacity? Why?	C5
Level 6 (Creating)	Combine parts to make a logical or functioning whole: element reorganization into a new pattern or structure (hypothesizing, designing, producing).	How would you design a floor plan that meets the needs of your client?	C6
Knowledge Dime	nsion		
Factual Knowledge	The knowledge contains the basic elements that students must master if they are to be introduced to a discipline or solve any problem.	<ul> <li>Please fill in the blanks below.</li> <li>A quadrilateral has interior angles.</li> <li>A triangle has three and</li> </ul>	K1
Conceptual Knowledge	The knowledge that is able to make connections between basic elements that form a broader structure and perform functions together.	In which of the following cases, a triangle cannot be drawn? A. $ BC  = 7 \text{ cm}, m \angle B = 64^{\circ}, m \angle C = 78^{\circ}$ B. $ DF  = 7 \text{ cm},  EF  = 9 \text{ cm}, m \angle F = 90^{\circ}$ C. $m \angle A = 56^{\circ}, m \angle B = 38^{\circ}, m \angle C = 86^{\circ}$ D. $ LM  = 14 \text{ cm},  KL  = 10 \text{ cm},  KM  = 9 \text{ cm}$	K2
Procedural Knowledge	Knowledge of how to do things, methods of inquiry, and criteria for using skills, algorithms, techniques, and methods to solve new problems.	The table below indicates that the four companies sell the same types of products in varying amounts, and discounts are applied to these prices. Which product, according to the table, is the best to buy? Discuss your choice with your friends.CompanyQuantitySales (kg)A57,000B811,000C1214,000D1524,000	K3

Level	Description	Example <sup>*</sup>	Code
Dimensions of C	ognitive Process		
Metacognitive Knowledge	Knowledge of cognition in general as well as awareness of their own cognition.	<ul> <li>Based on the number pattern 7, 12, 17, 22,</li> <li>a) Create a model of this pattern and discuss it.</li> <li>b) Use the pattern rule's "number of representatives" to express yourself.</li> <li>c) Determine the pattern's 48th step.</li> </ul>	K4
* Examples C1 to	C6 are retrieved from https://mo	dules.sanfordinspire.org/wp-	

content/uploads/2016/07/Creating\_Questions\_to\_Target\_Levels\_of\_Thinking\_Resource.pdf

Table 1 shows that there are six levels of cognitive dimensions as well as four dimensions of knowledge. Each category is given a code, namely C1, C2, C3, C4, C5, C6 for the cognitive dimension and K1, K2, K3, K4 for the knowledge dimension. Each mathematical task is categorized based on the appropriate coding in the two dimensions.

The validity of the data was carried out by employing peer debriefing (Kaur et al., 2020), namely the third, fourth, and fifth authors analyzed each textbook object and manually coded them according to the agreed categories. The results of the coding are cross-checked with each other and discussed to equalize perceptions. The analysis was continued by conducting focus group discussions for all researchers. The stage began with the presentation of the results of the previous analysis. Then, other researchers checked randomly, especially on unique cases, and included those doubtful from the previous analysis. The analysis results are presented in a pie chart and show the percentage for each category.

#### Results

#### **Textbook overview**

The mathematics textbook that we studied consists of 216 pages and includes 6 (six) chapters, namely fractions, HCF (Highest Common Factor) & LCM (Least Common Multiple), approximations, plane figures, statistics, and angle measurement. Thus, one chapter includes geometry, namely shapes, which are in chapter 4. Chapter 4 is divided into 4 (four) subchapters, namely polygons, the perimeter of shapes, the area of shapes, and relationships between lines. The sub-materials are allocated as many as 54 pages (25%).

In the shapes chapter, there are 144 mathematical tasks (30.25%) of the total number in the textbook, which is 476 items. The items referred to here are worked examples and exercises. Many items are counted down to each sub-item. For example, number 1 has sub a, b, and c; then, three tasks will be counted (1a, 1b, 1c). However, the researchers also consider whether each sub-items influences each other, so it is counted as one item. From many mathematical

tasks and the allocation of pages for the topic of geometry in this book, there is an emphasis that geometry material is a quite essential material in the fourth-grade Elementary School Mathematics subject.

#### Cognitive demands on geometrical tasks

In this section, the researchers present the results of the analysis of a combination of examples and exercises contained in the textbook. The task analysis results based on the cognitive process dimensions of Bloom's taxonomy in 4th-grade mathematics textbooks are presented in Figure 1.



Figure 1. Task categories based on the Cognitive Process Dimension

Based on Figure 1, the most significant percentage of cognitive demands in the textbook is level applying, getting a portion of 69.44%. This percentage of more than 50% indicates that the distribution for variations in cognitive processes on geometrical tasks is still not varied. The task categories classified as C4, C5, and C6 only received 4.86%, 2.08%, and 0%, respectively. In other words, the demands of cognitive processes in this textbook, especially for the geometry task, are more oriented to lower-order thinking skills.

Reproduction is dominant because the making of examples and exercises is relatively easy rather than questions that require high-level skills. However, students do not get much valuable experience for the demands of future learning. Except for level 6, sample items from each level of cognition can be seen in Table 2.

Categories	Sample task in the mathematics textbook		
Remembering	2. Berilah nama pada jenis garis berikut!		
	a. D C		
	b. X Y		
	c. V • W		
	(p.147)		
	Translation: Name the following line types!		
Understanding	<ol> <li>Gambarlah bangun segibanyak pada kotak di bawah ini dengan ketentuan berikut!</li> </ol>		
	a. Empat bangun segi banyak beraturan berbeda.		
	1 2 3 4		
	(p.111)		
	Translation: 3. Draw a polygon in the box below with the following conditions!		
Applying	<i>a. Four different regular polygons</i> 7 Sebuah persegi panjang mempunyai panjang 15 cm dan lebar 10 cm. Hitunglah		
	keliling dan luas persegi panjang!		
	(p.155)		
	Translation:		
	A rectangle has a length of 15 cm and a width of 10 cm. Find the perimete		
Analyzing	<ul> <li>5. Beni ingin membuat taplak meja berbentuk persegi dari kain batik. Sisi pada taplak meja tersebut adalah 150 cm. Harga 1 m<sup>2</sup> kain batik Rp50.000,00. Berapakah luas kain batik yang dibutuhkan oleh Beni? Jika Beni membawa uang Rp150.000,00, berapakah uang kembalian Beni?</li> </ul>		
	(p.132)		

**Table 2.** Sample tasks in each cognitive process dimension

Categories	Sample task in the mathematics textbook		
	Translation:		
	Beni wants to make a square-shaped tablecloth from batik cloth. The side		
	on the tablecloth is 150 cm. The price of $1 \text{ m}^2$ of batik cloth is IDR 50,000.00. How much area of batik cloth does Beni need? If Beni brings		
	IDR 150,000.00, how much money will Beni change?		
Evaluating	<ol> <li>Sebuah bangun datar mempunyai sifat-sifat sebagai berikut:         <ol> <li>Mempunyai empat sisi sama panjang</li> <li>Mempunyai empat sudut sama besar</li> <li>Kedua diagonalnya sama panjang dan saling berpotongan tegak lurus</li> <li>Bangun datar yang mempunyai sifat-sifat tersebut adalah</li> </ol> </li> </ol>		
	A. Persegi C. belah ketupat		
	B. Persegi panjang D. jajar genjang		
	(p.197)		
	Translation		
	2 A shape has the following properties:		
	1) It has four equal sides		
	2) It has four equal angles		
	3) The two diagonals are the same length and intersect at right angles to each other		
	A shape that has these properties is		
	A. Square C. Rhombus		

A. Square C. Rhombus B. Rectangle D. Parallelogram

Table 2 shows that there are only five dimensions of cognitive processes offered in mathematics textbooks: remembering, understanding, applying, analyzing, and evaluating, while for the creating level, we did not find them in the geometrical task. We are interested in discussing the sample tasks for level evaluation, which are shown in Table 2. Students are required to analyze, choose, and make decisions that match the defined criteria in this task. Because students are asked to evaluate the situation at hand, we have classified it as a level 5 activity. The point we wish to make is that the demands of students' thinking levels are not determined by the level of difficulty of the questions. Therefore, it is important to provide more easy tasks but require higher-order thinking skills.

#### The trend of knowledge offered in geometrical tasks

The analysis results on the dimensions of knowledge offered by the Grade 4 Elementary Mathematics Textbook are presented in Figure 2 below.



Figure 2. Task categories based on knowledge dimension

Figure 2 shows that procedural knowledge received the highest percentage, 60.42 percent. In other words, this knowledge encompasses 87 of the 144 items. Then came factual knowledge, which accounted for 20.14 percent, and conceptual knowledge, which accounted for 19.44 percent. This finding is consistent with our first finding, which revealed that most of the geometry tasks in this textbook are at the applying level. To solve the problems, procedural knowledge is required. However, the problem is that procedural knowledge is frequently insufficiently balanced with conceptual knowledge, making it challenging to tackle various problems (Purnomo et al., 2014, 2021; Purnomo, Widowati, et al., 2019). As a result, in teaching and learning practices, an overemphasis on exercise is more commonly dominating. Table 3 shows each sample task from each knowledge category.

Categories	Sample task in the mathematics textbook		
Factual Knowledge	2. Arsirlah bangun yang merupakan bangun segi banyak beraturan! a. b. c. d. d.		
	(p.154) <i>Translation:</i> Shada the shapes, which are regular polygons/		
	snaae me snapes, which are regular polygons!		

Table 3. Sample tasks in each knowledge dimension

Categories	Sample task in the mathematics textbook		
Conceptual	2. Sebuah bangun datar mempunyai sifat-sifat sebagai berikut:		
Knowledge	1) Mempunyai empat sisi san	na panjang	
	<ol> <li>Mempunyai empat sudut sama besar</li> <li>Kedua diagonalnya sama panjang dan saling berpotongan tegak lurus</li> <li>Bangun datar yang mempunyai sifat-sifat tersebut adalah</li> </ol>		
	A. Persegi	C. belah ketupat	
	B. Persegi panjang	D. jajar genjang	
	(p.197)		]
	<ol> <li>A shape has the following 1) It has four equal sides</li> <li>2) It has four equal angle</li> <li>3) The two diagonals are to each other</li> <li>A shape that has these provides</li> <li>A. Square</li> <li>C. Rhow</li> <li>B. Rectangle</li> <li>D. Parage</li> </ol>	properties: 25 the same length and intersect at right a operties is ombus vallelogram	ingles
Procedural Knowledge	<ul> <li>Ayah Meli akan membu seperti pada gambar di bar panjangnya 30 cm, bera yang dibutuhkan ayah Metersebut?</li> <li>Gambar 4.16 Tangga Bambu</li> <li>(p. 151)</li> <li>Translation:</li> <li>Mali's father will make a lade</li> </ul>	uat tangga dari bambu wah. Jika tiap ruas bambu apakah panjang bambu li untuk membuat tangga der out of hamboo, as in the picture bel	ow If

each segment of bamboo is 30 cm long, how much length of bamboo does Meli's father need to build the ladder?

Table 3 shows three dimensions of knowledge identified in our sample textbooks, while metacognitive knowledge was not identified in our analysis. The dominance of procedural knowledge is directly proportional to the dominance of cognitive processes for the level of application offered in this book. This finding is in line with the findings of Purnomo et al. (2019) on mathematics textbooks in junior high schools dominated by non-contextual problems so that the orientation and emphasis on procedural knowledge; focus on results than process.

#### Discussion

The findings of this study indicate that the mathematical tasks in the textbooks in this sample have not provided variations in cognitive demands, especially in the realm of higher-order thinking skills. The percentage of higher-order thinking skills indicates this; the ability to analyze, evaluate, and create is much lower than other lower levels of thinking. The most significant portion of the cognitive demands that textbooks provide is the level of application. The applying level in this textbook focuses more on students' ability to apply calculations and computations based on specific geometric rules, such as perimeter formulas, area formulas, and others. This level of application can be related to the term reproduction within the framework of the OECD (2010), which refers to fundamental knowledge and skills in applying mathematical concepts, rules, procedures, and representations (Gracin, 2018; Wijaya et al., 2015).

In line with the findings of the level cognitive portion, conceptual and metacognitive knowledge did not receive a proportional portion. The majority of what is presented in textbooks is procedural knowledge. A critique of our learning orientation requires students to think critically and face global changes and progress happening so fast. Children also need this ability in its application in everyday life and their work in the future, whether directly related to mathematics or not. Although some problems have presented contextual tasks, the orientation is still on procedural knowledge and includes realistic rather than authentic contexts. The authentic context is closer to the reader in everyday life, while the realistic context is more to the author's imagination in providing examples of everyday life so that sometimes it does not happen (Gracin, 2018; Purnomo, Mastura, et al., 2019).

Furthermore, Purnomo et al. (2019) state that authentic context-related tasks allow students to build a sense of the subject and real-life connections while engaging in mathematics examples and exercises fostering concept construction. This context can be exemplified in the sample task for procedural knowledge (see Table 2). The bamboo is composed of pieces of bamboo that are not found in real life, so it is purely the imagination of the author of the book. It is recommended that contextual features be offered proportionally, both in the dimensions of authentic, realistic, and intra-mathematical context (non-context).

Indonesian mathematics textbooks, described as low-level cognitive knowledge and skills, need to look at mathematics textbooks in countries with more advanced education. Based on related studies synthesized by (Yang & Sianturi, 2017), Singapore mathematics textbooks can be used to reference cognitive demands that require high-level skills. For example, for probability and statistics material, the cognitive demands are higher than for American (c.f., Siregar, 2015) and Indonesian textbooks; and for linear function material, which has higher cognitive demands than American textbooks (c.f., Fowler, 2015).

The complexity of the relationship between the dimensions of cognitive processes and knowledge is also identified in this study. The complexity in examples and exercises is a relationship not necessarily directly proportional and random between the two dimensions. For example, we found that one task was in conceptual knowledge, but it was at the evaluating level on the cognitive process dimension. We also found several examples of tasks at the applying level, not only at the procedural knowledge but also at the conceptual level. This focus can also

be found in relevant studies (Kar et al., 2018; Kul et al., 2018; Yang & Sianturi, 2017) but have not explored what, why, and how these two dimensions of cognition and knowledge related empirically. Therefore, it would be more meaningful if the following researchers could explore this more deeply by considering the diverse samples and the inquiry method.

### Conclusion

A textbook is a teaching material used by teachers and students to guide teaching and learning in the classroom. It is equipped with learning objectives so that the teaching and learning process can be carried out properly according to learning outcomes. Our study on mathematics textbooks focuses on topic shapes in grade 4 elementary school. The findings of this study indicate that most of the tasks provided by textbooks tend to lead to the orientation of low-level thinking skills and procedural thinking. More than 50% of tasks demand the ability to apply and provide questions with procedural knowledge orientation. Therefore, textbooks should and will be more meaningful when the variation of cognition and knowledge is more varied and proportional.

In addition to the above-mentioned findings, we also identified a complex relationship between the dimensions of cognitive processes and knowledge. Therefore, future researchers can explore this relationship more deeply, methodically, and with sample diversity. Furthermore, our research is limited to how textbooks are presented in a single curriculum context. When the analysis involves a comparative study of curricula that have been used in one country or a comparison of curricula in several countries with more advanced education, it is very comprehensive and has a broad meaning.

#### **Conflicts of Interest**

The authors declare that no conflict of interest regarding the publication of this manuscript. In addition, the ethical issues, including plagiarism, misconduct, data fabrication and/or falsification, double publication and/or submission, and redundancies have been completely by the authors.

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